

# Top quark mass effects in Higgs boson pair production at the LHC

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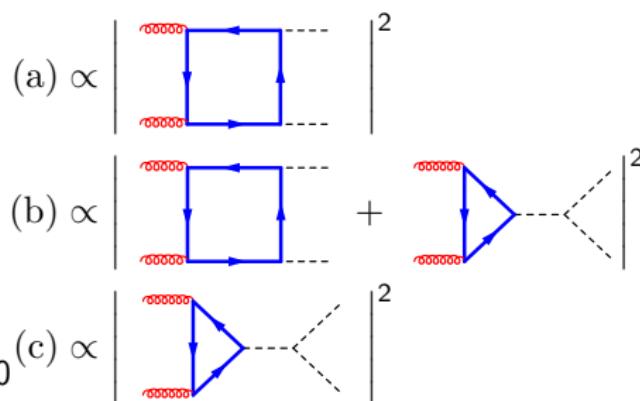
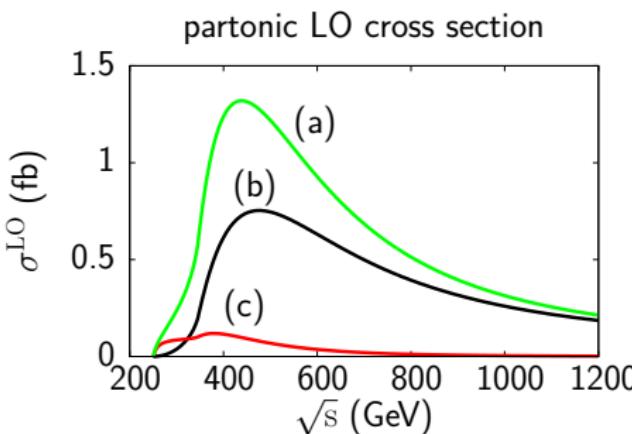
Nucl. Phys. B875 (2013), arXiv:1305.7340

LoopFest XIII  
New York City College of Technology  
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# Motivation

Higgs potential in the Standard Model

$$V(H) = \frac{1}{2}m_H^2 H^2 + \lambda v H^3 + \frac{1}{4}\lambda H^4 \quad \lambda = \frac{m_H^2}{2v^2} \approx 0.13 \quad v = \text{Higgs vev}$$



# Measurement at the (14 TeV) LHC

- $b\bar{b}\gamma\gamma$  channel,  $600 \text{ fb}^{-1}$ :  $\lambda \neq 0$  [Baur, Plehn, Rainwater '04]
- $b\bar{b}\gamma\gamma$ ,  $b\bar{b}\tau^+\tau^-$  channel: “promising”  
 $b\bar{b}W^+W^-$  channel: “not promising”  
[Baglio, Djouadi, Gröber, Mühlleitner, Quevillon, Spira '13]
- ratio of double Higgs / single Higgs cross sections  
 $600 \text{ fb}^{-1}$ :  $\lambda > 0$   
 $3000 \text{ fb}^{-1}$ :  $\lambda^{+30\%}_{-20\%}$   
[Goertz, Papaefstathiou, Yang, Zurita '13]
- $b\bar{b}\gamma\gamma$  channel,  $3000 \text{ fb}^{-1}$ :  $\lambda \pm 40\%$   
[Barger, Everett, Jackson, Shaughnessy '14]
- and many more, e.g.:  
[Papaefstathiou, Yang, Zurita '13]  
[Dolan, Englert, Spannowsky '12]

# Theory status

- LO with full  $m_t$  dependence [Glover, van der Bij '88; Plehn, Spira, Zerwas '98]
- NLO in the limit  $m_t \rightarrow \infty$  [Dawson, Dittmaier, Spira '98]
- NNLO<sup>approx.</sup> in the limit  $m_t \rightarrow \infty$  [de Florian, Mazzitelli '13]
- resummation [Shao, Li, Li, Wang '13]
- matched and merged [Maierhöfer, Papaefstathiou '13; Li, Yan, Zhao '14; Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Torrielli, Vryonidou, Zaro '14]
- ...

$$\sigma_{\text{total, hadronic}} \approx (20^{\text{LO}} + 20^{\text{NLO, } m_t \rightarrow \infty} + 8^{\text{NNLO, } m_t \rightarrow \infty}) \text{ fb}$$

$$(\sqrt{s_{\text{had}}} = 14 \text{ TeV}, \mu = 2m_H)$$

this talk: NLO corrections of  $\mathcal{O}(1/m_{\text{top}}^n)$

# Calculation via optical theorem

$$\sigma_{\text{total}}(\text{gg} \rightarrow \text{HH}) \propto \text{Disc}(\mathcal{M}(\text{gg} \rightarrow \text{gg}))$$

$$\int dPS \left| \begin{array}{c} \text{Diagram 1} \\ + \\ \text{Diagram 2} \end{array} \right|^2 \propto$$

$$\begin{array}{c} \text{Diagram 3} \\ + \\ \text{Diagram 4} \\ + \\ \text{Diagram 5} \end{array}$$

- pro
- calculating  $\text{Disc}(\dots)$  possible at master integral level
  - simplified kinematics
  - master integrals and phase space integration at once

- con
- more loops, more diagrams
  - only total cross section

# Feynman diagrams

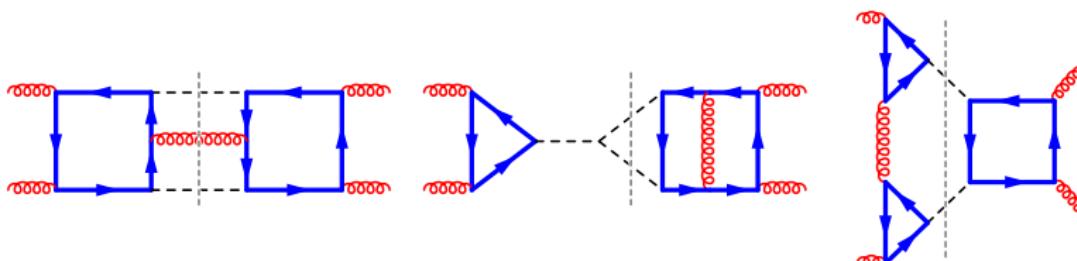
## gluon-gluon channel

- virtual corrections

- $gg \rightarrow hh$   
126 two loop diagrams
- cross check:  $gg \rightarrow gg$   
1052 four loop diagrams

- real corrections

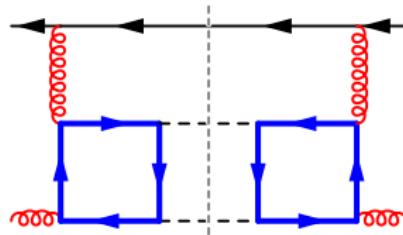
- $gg \rightarrow gg$   
1530 four loop diagrams



# Feynman diagrams

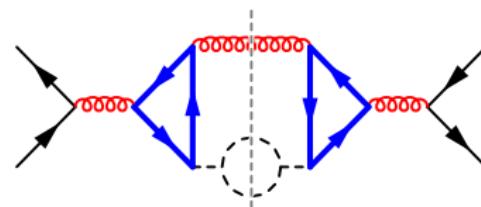
## quark-gluon channel

- $qg \rightarrow qg$   
34 four loop diagrams



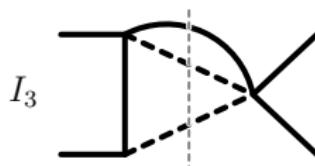
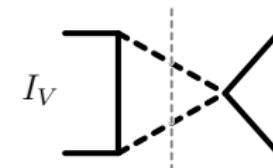
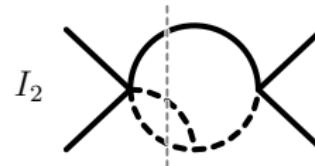
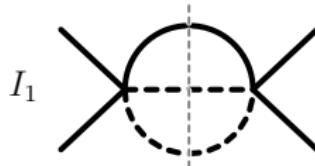
## quark-anti-quark channel

- $q\bar{q} \rightarrow q\bar{q}$   
34 four loop diagrams

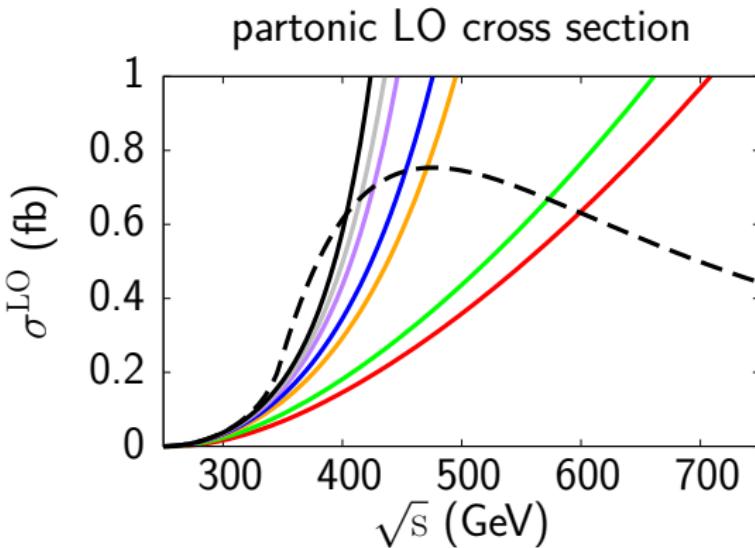


# Master integrals

- at NLO: 4 (real) + 1 (virtual) master integrals
- $2 \rightarrow 3$  and  $2 \rightarrow 2$  phase space integrals
- dependent on  $s = (q_1 + q_2)^2$  and  $m_H$
- simplification: expansion in  $\delta = 1 - \frac{4m_H^2}{s}$  at least up to  $\mathcal{O}(\delta^{50})$ 
  - converges very well
  - no visible numerical effect on cross section



# Expansion in $1/m_t$



dashed line exact in  $m_t$

solid lines expansion in  $1/m_t$

$$\rho = \frac{m_H^2}{m_t^2} \approx 0.5$$

$$\rho^0 \ \rho^1 \ \rho^2 \ \rho^3 \ \rho^4 \ \rho^5 \ \rho^6$$

scales:

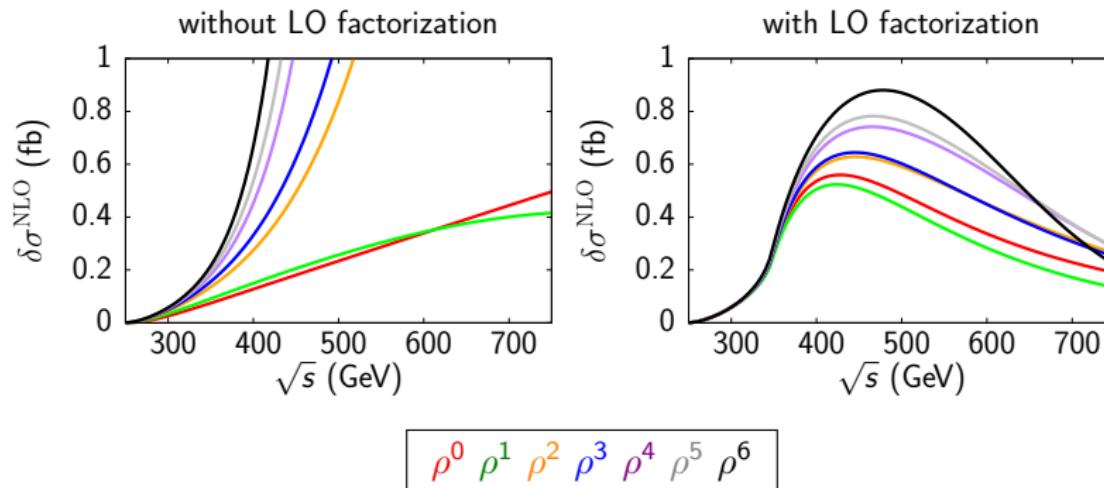
$$m_t = 173 \text{ GeV}$$

$$m_H = 126 \text{ GeV}$$

$$\sqrt{s} \geq 252 \text{ GeV}$$

# Partonic cross sections: gluon-gluon channel

Factorization of exact LO cross section

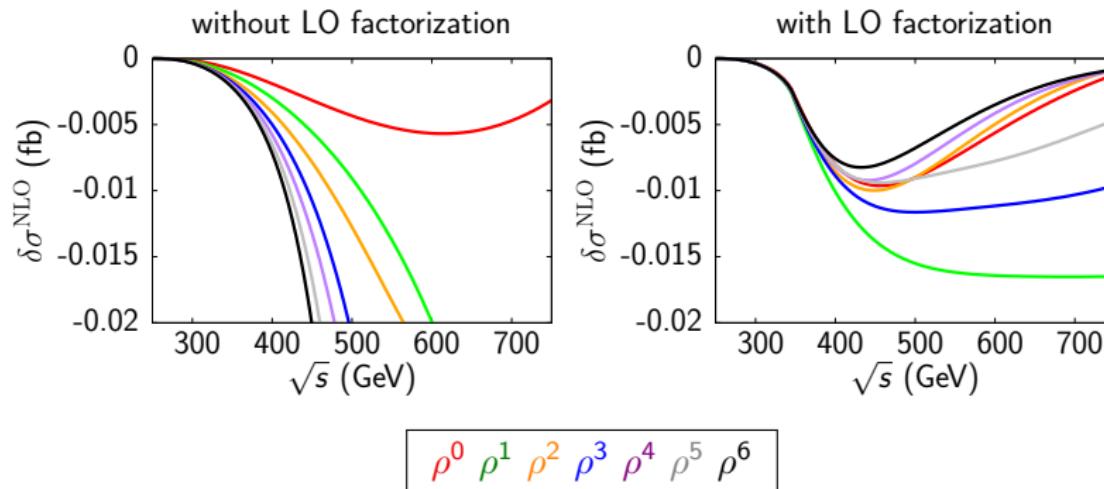


factorize exact LO cross section

$$\sigma_{\text{expanded}}^{\text{NLO}} \rightarrow \sigma_{\text{exact}}^{\text{LO}} \frac{\sigma_{\text{expanded}}^{\text{NLO}}}{\sigma_{\text{expanded}}^{\text{LO}}}$$

# Partonic cross sections: quark-gluon channel

Factorization of exact LO cross section

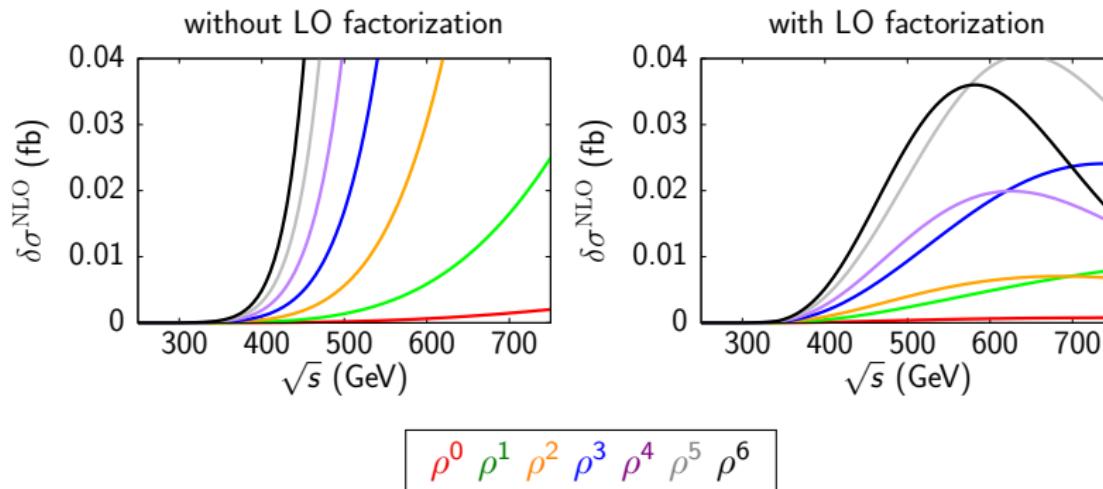


factorize exact LO cross section

$$\sigma_{\text{expanded}}^{\text{NLO}} \rightarrow \sigma_{\text{exact}}^{\text{LO}} \frac{\sigma_{\text{expanded}}^{\text{NLO}}}{\sigma_{\text{expanded}}^{\text{LO}}}$$

# Partonic cross sections: quark-anti quark channel

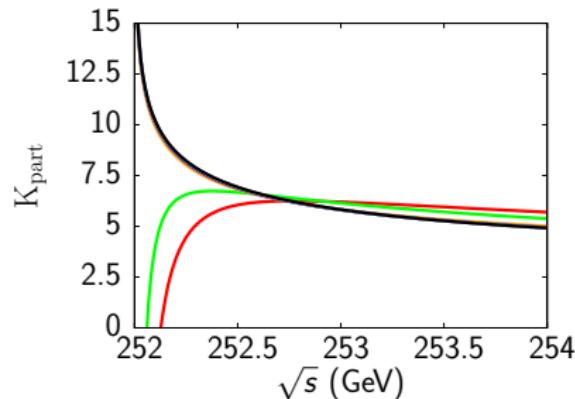
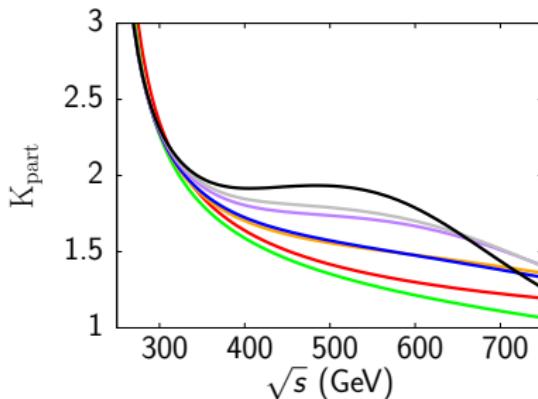
Factorization of exact LO cross section



factorize exact LO cross section

$$\sigma_{\text{expanded}}^{\text{NLO}} \rightarrow \sigma_{\text{exact}}^{\text{LO}} \frac{\sigma_{\text{expanded}}^{\text{NLO}}}{\sigma_{\text{expanded}}^{\text{LO}}}$$

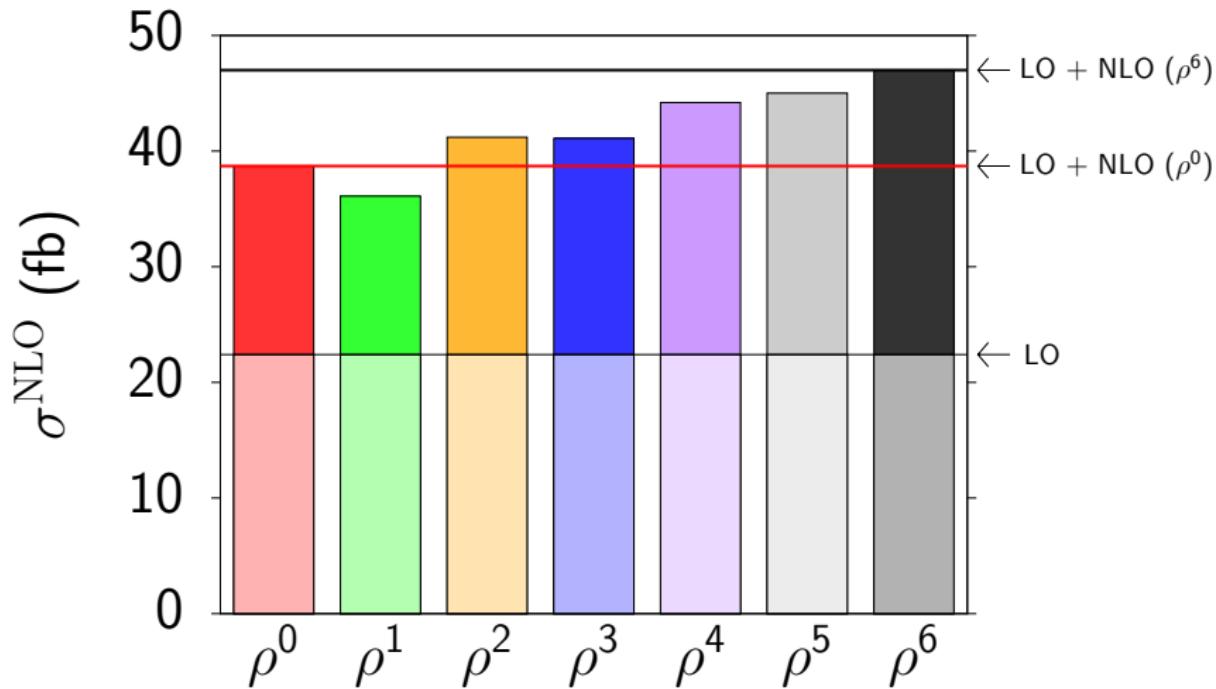
# K-factors



- strong enhancement for  $\sqrt{s} \lesssim 400$  GeV  
(remember: LO cross section vanishes at threshold)
- close to threshold highly dependent on  $\mathcal{O}(\rho)$

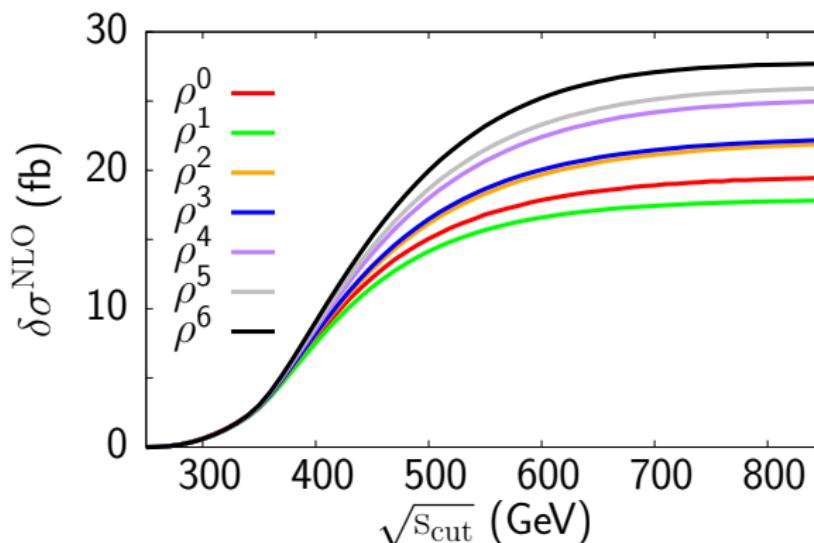
# Total hadronic cross section (all channels)

MSTW2008 pdfs,  $\sqrt{s_{\text{had}}} = 14 \text{ TeV}$ ,  $\mu = 2m_H$

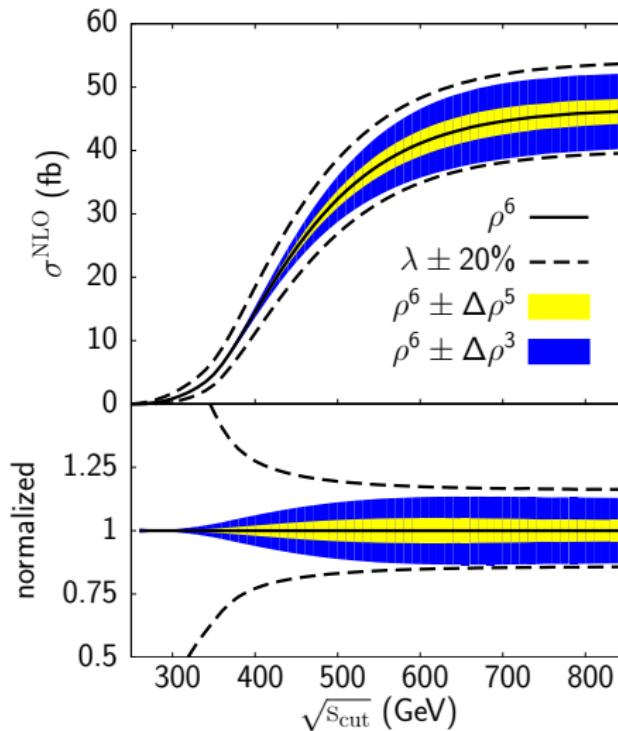


# Behavior for low $\sqrt{s}$ : estimation of $Q^2$ distribution

- virtual corrections:  $\sqrt{s} = \sqrt{Q^2}$  (invariant mass of Higgs pair)
- soft real corrections:  $\sqrt{s} \approx \sqrt{Q^2}$
- observation: cross section dominated by soft and virtual corrections



# Sensitivity to triple Higgs coupling



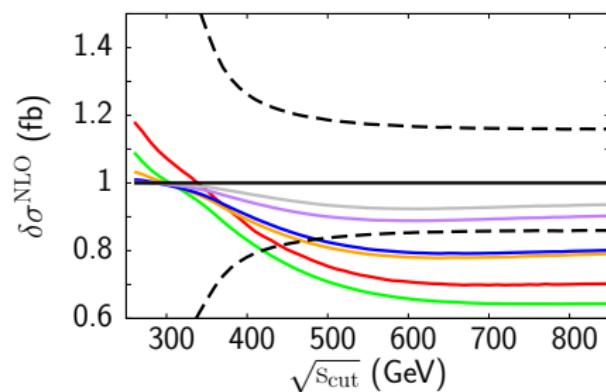
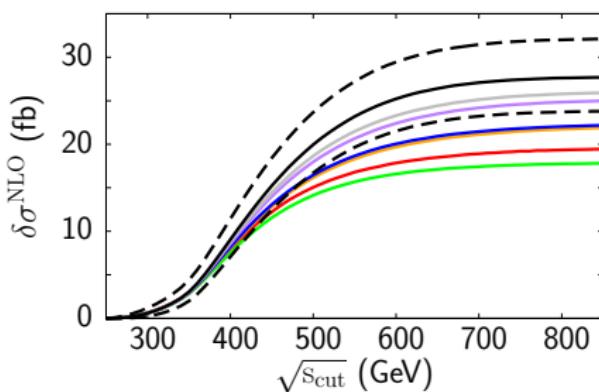
# Conclusion

- $\sigma(pp \rightarrow HH)$  in the SM at NLO including  $\mathcal{O}(1/m_t^{12})$  terms
- independent check of  $m_t \rightarrow \infty$  result [Dawson, Dittmaier, Spira '98]
- top mass corrections are numerically important:  
+20% compared to  $\sigma^{\text{NLO}}(m_t \rightarrow \infty)$
- quantitative estimate of remaining  $\mathcal{O}(1/m_t^n)$  uncertainties

backup

# Hadronic cross section

MSTW2008 pdfs,  $\sqrt{s_{\text{had}}} = 14 \text{ TeV}$ ,  $\mu = 2m_H$



# Hadronic cross section - numbers

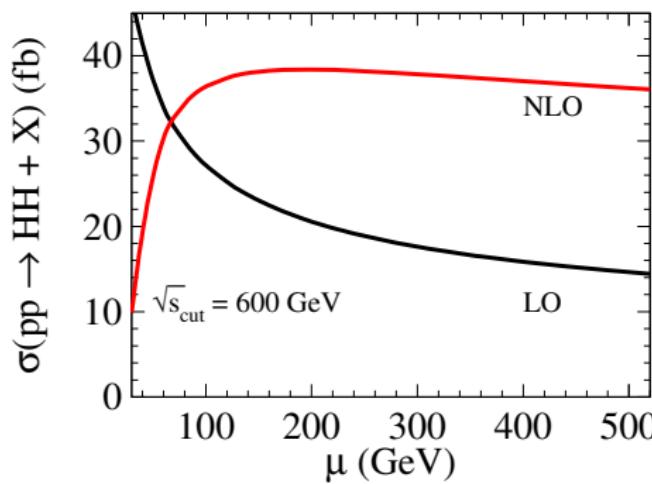
MSTW2008 pdfs,  $\sqrt{s_{\text{had}}} = 14 \text{ TeV}$ ,  $\mu = 2m_H$

total hadronic cross section in fb, all channels

LO	$\delta\text{NLO}$	$\rho^0$	$\rho^1$	$\rho^2$	$\rho^3$	$\rho^4$	$\rho^5$	$\rho^6$	LO + $\delta\text{NLO}$
19.7 (22.4*)	19.0	16.4	21.5	21.4	24.5	25.3	27.3	47.0	

\* with LO pdfs

# Scale dependence



$$\mu = \mu_F = \mu_R$$

$$\mu_{\text{central}} = 2m_H$$

$$\sigma^{\text{LO}} = 18^{+6}_{-4} \text{ fb}$$

$$\sigma^{\text{NLO}} = 38^{+0}_{-2} \text{ fb}$$

# Used software

- 1 create diagrams: QGRAF [Nogueira '93]
- 2 select diagrams with appropriate cuts [Hoff, Pak (unpublished)]
- 3 asymptotic expansion: Q2E and EXP  
[Harlander, Seidensticker, Steinhauser '98]
- 4 reduction to scalar integrals: (T)Form  
[Vermaseren '90; Tentyukov, Vermaseren '10; Kuipers, Ueda, Vermaseren, Vollinga '13]
- 5 reduction to master integrals: FIRE [Smirnov '08, '13]